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# A modifed and weighted Gower distance-based clustering analysis for mixed type data: a simulation and empirical analyses

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# **Abstract**

**Background** Traditional clustering techniques are typically restricted to either continuous or categorical variables. However, most real-world clinical data are mixed type. This study aims to introduce a clustering technique specifcally designed for datasets containing both continuous and categorical variables to offer better clustering compatibility, adaptability, and interpretability than other mixed type techniques.

**Methods** This paper proposed a modifed Gower distance incorporating feature importance as weights to maintain equal contributions between continuous and categorical features. The algorithm (DAFI) was evaluated using fve simulated datasets with varying proportions of important features and real-world datasets from the 2011–2014 National Health and Nutrition Examination Survey (NHANES). Efectiveness was demonstrated through comparisons with 13 clustering techniques. Clustering performance was assessed using the adjusted Rand index (ARI) for accuracy in simulation studies and the silhouette score for cohesion and separation in NHANES. Additionally, multivariable logistic regression estimated the association between periodontitis (PD) and cardiovascular diseases (CVDs), adjusting for clusters in NHANES.

**Results** In simulation studies, the DAFI-Gower algorithm consistently performs better than baseline methods according to the adjusted Rand index in settings investigated, especially on datasets with more redundant features. In NHANES, 3,760 people were analyzed. DAFI-Gower achieves the highest silhouette score (0.79). Four distinct clusters with diverse health profles were identifed. By incorporating feature importance, we found that cluster formations were more strongly infuenced by CVD-related factors. The association between periodontitis and cardiovascular diseases, after adjusting for clusters, reveals signifcant insights (adjusted OR 1.95, 95% CI 1.50 to 2.55, *p*=0.012), highlighting severe periodontitis as a potential risk factor for cardiovascular diseases.

**Conclusions** DAFI performed better than classic clustering baselines on both simulated and real-world datasets. It efectively captures cluster characteristics by considering feature importance, which is crucial in clinical settings where many variables may be similar or irrelevant. We envisage that DAFI offers an effective solution for mixed type clustering.

**Keywords** Clustering, Distance measure, Feature importance, Mixed type data

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# **Background**

 Data-driven population segmentation in clinical settings separates heterogeneous populations into homogenous groups with similar disease burdens and healthcare features [\[1](#page-13-0)]. Diferent care plans can be designed for each population subgroup using population segmentation [\[2](#page-13-1)]. Healthcare resource planning and evidence-based policymaking are both improved by using population segmentation analysis [[3\]](#page-13-2). However, conventional segmentation has faced challenges due to the cost of patient information collection, which often involves time-consuming and labor-intensive processes such as manual data entry and extensive medical examinations. Electronic health records (EHRs) and population health surveys have become primary sources for clinical research, enhancing segmentation with their accessibility and granularity [\[3](#page-13-2)]. Clustering analysis is widely used for data-driven segmentation [\[1](#page-13-0)] but struggles with mixed type data, which includes both continuous and categorical variables. Traditional clustering algorithms, like k-means, are limited to continuous variables, posing challenges when dealing with mixed type data [\[4\]](#page-13-3).

Clustering mixed type data in biomedicine holds signifcant value due to its ability to address complex and heterogeneous data sets [[5\]](#page-13-4). It enables patient stratification [[6\]](#page-13-5), pattern discovery in genomics [[7\]](#page-13-6), personalized medicine [[8\]](#page-13-7), disease marker identifcation [[9\]](#page-13-8), and linking genetics with brain imaging [\[10](#page-13-9)]. Another important beneft of clustering is to help gain diferent insights into associations among people sharing similar baseline characteristics [\[11](#page-13-10)].

Analysts have attempted to transform mixed type data into a uniform type for clustering [[12,](#page-13-11) [13](#page-13-12)], for example, converting all variables into continuous ones and using k-means to calculate Euclidean distances [[14](#page-13-13), [15](#page-13-14)]. But this transformation often results in a loss of information, impairing segmentation quality. The k-prototypes algorithm [\[16](#page-13-15)], an adaptation of k-means, combines squared Euclidean and matching distances to cluster mixed data. User-defned weighting factors set the importance of each variable type, echoing the limitations of using Gower's distance. However, most previous weighting methods don't fully address the challenges of mixed data [\[17,](#page-13-16) [18](#page-13-17)], often failing to balance the infuence of continuous and categorical variables efectively [\[19](#page-13-18), [20\]](#page-13-19).

Model-based clustering assumes data comes from various probability distributions, with each representing a different cluster  $[21-23]$  $[21-23]$  $[21-23]$ . This method is effective for mixed-type datasets where other clustering techniques struggle [[24](#page-13-22)]. It uses distributions (like Gaussian or multinomial) to model clusters and the Expectation-Maximization (EM) algorithm to estimate distribution parameters and assign data points to clusters [[25](#page-13-23)]. While adaptable and useful for determining cluster membership probabilities and the number of clusters, it can falter if its assumptions are not met.

KAMILA [\[26](#page-13-24)] (KAymeans for MIxed Large data), an efficient variant of the k-means algorithm  $[15]$  $[15]$ , addresses the challenge of clustering mixed continuous and categorical data without heavy parametric assumptions [\[23](#page-13-21)]. Simulation results indicate that it handles large datasets efectively, addressing both data types without explicit weighting, with potential advantages over methods such as normal-multinomial mixture models and the Modha-Spangler weighting approach in certain contexts [[27](#page-13-25), [28\]](#page-13-26).

In addition to clustering algorithms, many distance metrics were proposed for mixed type data, which integrate diferent types of variables' distance, with Gower's distance being the most popular [\[29](#page-13-27)]. However, Gower distance can be dominated by categorical variables, neglecting the important diferences within variable types  $[30]$ . This paper explores the efficacy of current clustering techniques for handling mixed type data and identifes a gap in using Gower distance to consider the infuence of both continuous and categorical variables evenly.

To address this gap, we introduce an innovative twostep framework for mixed type clustering with a new modifed and weighted Gower distance, DAFI-Gower, considering distance adjustment and feature importance to improve clustering quality and interpretability. The performance of the DAFI-Gower method was evaluated using simulated data and compared with other mixed type clustering techniques to assess clustering quality. Additionally, its application was demonstrated using real-world datasets to identify distinct health profles, particularly those related to periodontitis (PD) and cardiovascular diseases (CVDs). The method also aids in adjusting for confounders in association analyses through clustering.

# **Methods**

This section details our proposed two-step framework: frst, a distance matrix is constructed to quantify a balanced distance measurement between diferent types of variables; second, a clustering algorithm is applied using this distance matrix. The distance matrix employs our modifed Gower distance, incorporating distance adjustment and mutual information-based feature importance (DAFI) weights.

# **Gower distance**

Distance metrics created for mixed data sets, such as Gower distance [\[29](#page-13-27)], are widely used for measuring the degree of dissimilarity between observations when mixed type features are present. Assume a mixed type dataset *X* with *n* observations has *p* features, where the frst *h* features are continuous, and the remaining features from  $h+1$  to  $p$  are categorical. Therefore, the Gower distance between two observations  $x_i = (x_{1i}, x_{2i}, \ldots, x_{ji}, \ldots, x_{pi})$ and  $\mathbf{x}_k = (x_{1k}, x_{2k}, \dots, x_{jk}, \dots, x_{pk})$  from dataset *X (i, k*∈ {1,2, ... , n}*)* is:

$$
d(\pmb{x_i}, \pmb{x_k}) = \frac{1}{p} \left\{ \sum \frac{p}{j=1} d_j(x_{ji}, x_{jk}) \right\},\,
$$

where  $d_j(x_{ji}, x_{jk})$  is defined differently for continuous and categorical variables:

$$
d_j(x_{ji}, x_{jk}) = \begin{cases} \frac{|x_{ji} - x_{jk}|}{R_j} & \text{if } j \in \{1, 2, \ldots, h\} \\ I(x_{ji} \neq x_{jk}) & \text{if } j \in \{h+1, h+2, \ldots, p\}, \end{cases}
$$

where  $R_j$  is the range for the value of  $j<sup>th</sup>$  continuous feature, with  $x_{ji}$  and  $x_{jk}$  being the values of the  $j^{th}$  feature for observations  $x_i$  and  $x_k$  separately.  $I(x_{ji} \neq x_{jk})$ is 1 if  $x_{ji} \neq x_{jk}$  and 0 otherwise. The default setting in Gower distance specifes equal weights for all variables, while a vector of variable importance could be applied to  $d_i(x_i, x_k)$  as an optional choice. Gower distance in a clinical context compares patients by assigning higher weights to more critical variables, such as focusing on recovery time and complications for evaluating treatment outcomes [[31](#page-13-29)], ensuring that these attributes have a greater infuence on the similarity calculation for more accurate patient comparisons.

In conventional Gower distance calculation, categorical variables often impact the results more than continuous ones because a categorical diference can easily reach the maximum distance of 1. In contrast, the diference in a continuous variable only reaches 1 when calculated between the extremes (minimum and maximum values). This discrepancy can cause categorical variables to disproportionately infuence the distance metric and afect subsequent analysis, as categorical diferences are more common and can overshadow the nuanced diferences captured by continuous variables. For instance, two individuals with a 63-year age diference (continuous) may have a smaller Gower distance than those difering only by sex (categorical).

To address the imbalance in Gower distance calculations, D'Orazio [\[30](#page-13-28)] suggested using the inter-quartile range (IQR) for continuous variables to reduce outlier impacts and balance variable contributions but not having similar adjustments made for categorical variables.

# **Proposed modifed Gower distance**

To improve the handling of categorical variables, we converted categorical values into dummy variables to refne the distance measure, aligning it with continuous variables (Fig. [1](#page-3-0)). However, this method can disproportionately afect datasets with variables that have many categorical levels. To address this, adjusted weights were proposed for categorical features using continuous features as references, and for continuous features, scaling the Manhattan distance (the absolute diference) by the IQR is kept using as recommended by D'Orazio [\[30](#page-13-28)]. This method achieves a more fine-grind and balanced assessment of dissimilarity for mixed type variables, ensuring continuous and categorical features contribute equitably to the overall distance measure. Below are the details for calculating weights.

## *Continuous features*

For each continuous feature, the sum of the absolute diferences is calculated between all possible pairs of observations. Mathematically, for each feature column  $X_i (j \in \{1,2,\ldots,h\})$ , the sum of distances is given by:

$$
D_{X_j} = \sum_{i=1}^n \sum_{k=1}^n |X_{ji} - X_{jk}|
$$

where  $n$  is the number of observations. Then, the calculated sum distance is divided by the diference between the first and third quartiles  $[30]$  $[30]$ . Mathematically:

$$
Q_{X_j}=\frac{D_{X_j}}{Q_3(X_j)-Q_1(X_j)}
$$

where  $\mathrm{Q}_{3}(X_{j})$  and  $\mathrm{Q}_{1}(X_{j})$  are the third and first quartiles of the  $j<sup>th</sup>$  continuous feature.

#### *Categorical features*

Each categorical feature  $X_i$ ,  $(j \in \{h+1, h+2, \ldots, p\}),$ with *L* levels is converted into *L* dummy variables first, where  $X_{j[m]}$  denotes the  $m^{th}$  dummy variable  $(m \in \{1,2,\ldots,L\})$ . Then, the sum of the differences is calculated for all *L* dummy variables between each pair of observations. Mathematically, for each feature column  $X_i$ , the sum of distances is given by:

$$
D_{X_j} = \left\langle \sum_{i=1}^n \sum_{k=1}^n \sum_{m=1}^L \left\{ I\left(x_{(j[m])i} \neq x(j[m])k\right) \right\} \right\rangle / L
$$

where  $x_{(j[m])i}$  is the m<sup>th</sup> dummy variable of categorical feature  $X_j$  for the  $i^{th}$  observation, and L is the total number of dummy variables for the categorical feature  $X_i$ . Then, the distance is averaged by the number of dummy variables *L*. An example for comprehension is available in Supplementary Fig. 1.

As mentioned earlier, the adjusted distance for categorical variables is calculated then. This is done by scaling the original distance  $D_{X_j}$  for categorical variables. We multiply by the scaling factor  $(\alpha_i)$ , which is the ratio of the average of normalized distances for the continuous



<span id="page-3-0"></span>**Fig. 1** The overall framework of the DAFI-Gower algorithm used for mixed type clustering

features  $Q_{X_q}(q \in \{1,2,\ldots,h\})$  to the categorical features  $D_{X_i} (j \in \{h+1, h+2, \ldots, p\})$ :

$$
\alpha_j = \frac{\frac{1}{h}\sum_{q=1}^h Q_{X_q}}{D_{X_j}} = \frac{\overline{Q_X}}{D_{X_j}}
$$

As previously mentioned,  $Q_{X_q}$  and  $D_{X_j}$  represent total distance contributed by a continuous feature  $X_q$  and a categorical feature  $X_i$ , respectively, they can be interpreted as the contributions to the overall distance. Therefore, with the scaling factor  $\alpha_i$  in the modified Gower distance to adjust the  $D'_{X_j} = \alpha_j x D_{X_j} = \overline{Q}_X$ , we guarantee the balanced contribution of continuous and categorical features toward the total distance.

# <span id="page-3-1"></span>**Proposed modifed and weighted Gower distance with feature importance**

After aligning the distance measures for continuous and categorical features, the modifed Gower distance matrix is used for clustering. Clustering quality and interpretations are critical, especially in clinical settings. Therefore, identifying key features is crucial for efective analysis, moving beyond mere grouping subjects to determining which features signifcantly infuence group formation. This improves clustering interpretations by addressing the limitations of its unsupervised nature. Therefore,

incorporating feature importance as weights was proposed in the modifed Gower distance to obtain the fnal dissimilarity matrix.

Information theory concepts like entropy and mutual information (MI) are crucial for evaluating feature importance [\[32](#page-13-30)]. Before the calculation of entropy and MI, continuous variables are converted into categorical variables based on quartiles  $[19, 33]$  $[19, 33]$  $[19, 33]$ . Entropy  $(H(X))$  measures the uncertainty of a discrete variable, indicating higher information content with greater unpredictability [[34\]](#page-14-1). Furthermore, MI  $(I(X_1; X_2))$  measures how much knowing one variable reduces the uncertainty of another, which is crucial for selecting relevant features by quantifying the information shared between variables. However, MI can suffer from redundancy, capturing overlapping information from multiple variables and overestimating their importance [[35\]](#page-14-2). Normalized MI (NMI), a variant of MI, addresses this by providing better accuracy and handling redundancy [[36\]](#page-14-3). It is defined as:

$$
NMI(X_1; X_2) = \frac{I(X_1; X_2)}{max\{H(X_1), H(X_2)\}}
$$

Horibe [\[37\]](#page-14-4) demonstrated that MI scaled by the maximum of entropy is a valid distance metric, making it a normalized similarity metric [\[38](#page-14-5)]. Mousavi and Elahe [[39\]](#page-14-6) also introduced a unified framework based on

mutual information control variables' contribution to distance measurement, which could prevent unnecessary information. Therefore, to measure feature importance, the average NMI of each feature with all other features was proposed as the weighting parameter  $\omega$ . Procedures for calculating the weighting parameter  $\omega$  for the  $j^{th}$  feature are shown below (Algorithm 1). In detail, for each feature *j*, the algorithm calculates how much information it shares with every other feature using NMI. The total NMI score for feature *j* is then averaged and stored in a vector. Finally, the importance weights are normalized by dividing the sum of all weights, ensuring they add up to 1.

Algorithm 1 Pseudo-code for feature importance weights

# $NMI = 0_{ncol(X)}$ for  $j = 1$  to  $\text{ncol}(X)$  do  $X_{*j} = X[ , -j]$  $X_i = X[, j]$  $Weight_i = 0$ for  $m = 1$  to  $\text{ncol}(X_{*i})$  do  $Weight_i = Weight_i + NMI(X_i, X_{*i}[, m])$ end for  $Weight_j = Weight_j / \text{ncol}(X_{*j})$  $\mathbf{NMI}[j] = Weight_j$ end for  $\omega = \text{NMI} / \text{sum}(\text{NMI})$ return  $\omega$

This approach considers both the intrinsic uncertainty of features and their mutual dependency on each variable. Therefore, the entire DAFI-Gower distance is calculated as:

rent framework employs PAM, it can accommodate any clustering algorithm that accepts a predefned distance matrix.

**The proposed study design using DAFI‑Gower algorithm** The novel mixed type clustering technique (Fig. [1](#page-3-0)) provides a balanced distance measurement and incorporates feature importance as weights. In the frst phase, the DAFI-Gower algorithm is designed to calculate the distance matrix through three main parts: calculating the modifed Gower distance, adjusting the distance with factor  $\alpha$ , and incorporating feature importance  $\omega$  as weights. The resulting DAFI-Gower distance matrix is then used for subsequent clustering analysis. Partitioning around medoids (PAM) [[40](#page-14-7), [41\]](#page-14-8)) is chosen, as it allows clustering based on a predefned distance matrix. While our cur-

$$
DAFI - Gower Distance = DAFI(x_i, x_k) = \frac{1}{p} \left\{ \sum_{j=1}^{p} \alpha_j * \omega_j * d_j(x_{ji}, x_{jk}) \right\},\,
$$

where  $d_j\big(x_{ji},x_{jk}\big)$  is calculated through:

$$
d_j(x_{ji}, x_{jk}) = \begin{cases} \frac{\sum_{i=1}^n \sum_{k=1}^n |x_{ji} - x_{jk}|}{IQR_j} & \text{if } j \in \{1, 2, \dots, h\} \\ \frac{\sum_{i=1}^n \sum_{k=1}^n \sum_{k=1}^L \{I(x_{(j[m])i} \neq x_{(j[m])k})\}}{L} & \text{if } j \in \{h+1, h+2, \dots, p\}, \end{cases}
$$

According to the formula for the DAFI-Gower distance, which involves summation terms, the calculation requires iterating over i (from 1 to n) for each k (also ranging from 1 to n). Therefore, for any given *L*, the time complexity is  $O(n^2)$ , indicating that as the size of the dataset (*n*) increases, the number of computations grows quadratically. Analysis was also conducted to compare the execution time of DAFI-Gower algorithm using NHANES.

# **Simulation settings**

Simulation studies were conducted to compare the accuracy of the proposed method against commonly used clustering techniques for mixed type data, evaluate improvements from diferent feature importance strategies, and assess scalability with heterogeneous datasets with diferent proportions of important features contributing to clustering (feature importance). The adjusted Rand index (ARI) was calculated

to measure the similarity between true and predicted clustering  $[42]$  $[42]$ , where ARI ranges from  $-1$  (indicating totally diferent) to 1 (indicating a perfect match), with 0 indicating the similarity between the two partitions is what would be expected by chance [[42](#page-14-9)].

Five simulation settings with diferent proportions of feature importance were generated (Supplementary Table 1), refecting real-world clinical scenarios with many redundant variables. Three underlying true clusters with cluster sizes of 60, 60, and 80 were assumed. Each study had fve continuous and fve categorical variables. Five continuous variables were drawn from normal distributions with cluster-specifc means and standard deviations. If the variable has the same mean for all clusters, it did not contribute to cluster formation. Additionally, fve categorical variables were generated with predefned categories and cluster-specifc probabilities. Similarly, if the variable has the same probabilities for all clusters, it had no contribution to cluster formation. Data points were assigned to clusters based on these parameters, resulting in distinct cluster profiles. This process was repeated 500 times to create datasets for further analysis. To validate the reproducibility of DAFI-Gower, we conducted additional simulations with cluster sizes of 30, 60, and 90, simulating scenarios with less balanced cluster sizes. All other parameters were kept consistent with the previous settings. The scenarios were:

- (1) 4/5 of both continuous and categorical variables contribute to clustering.
- (2) 3/5 of both continuous and categorical variables contribute.
- (3) 2/5 of both continuous and categorical variables contribute.
- (4) 1/5 of both continuous and categorical variables contribute.
- (5) 2/5 of continuous and 4/5 of categorical variables contribute.

Simulation scenario 5 was designed to refect realworld settings like social science and EHRs, where categorical variables usually dominate the datasets. For each setting, 500 datasets were generated. After using DAFI-Gower to calculate the distance matrix, we applied PAM for the clustering analysis.

In order to compare the overall performance of DAFI-Gower with commonly used mixed type clustering techniques, as well as evaluate each component's importance in DAFI-Gower, we designed simulation studies into three parts:

Part I: Comparison of DAFI-Gower with commonly used mixed type clustering techniques:

- (1) K-prototypes [[16\]](#page-13-15) (an adaptation of k-means, combines squared Euclidean and matching distances to cluster mixed data). This method was implemented by its authors in the *clustMixType* R package [\[43\]](#page-14-10);
- (2) K-means (categorical factors are treated as numeric; non-numeric categories are assigned arbitrary numeric codes for clustering);
- (3) K-modes (discretize all continuous variables into categorical ones based on quartiles; for example, given a continuous variable x, defne the quartile boundaries Q1 (25th percentile of x), Q2 (50th percentile of x), Q3 (75th percentile of x). Now, defne a new categorical variable  $x_{cat} = 1$  (if  $x \leq Q_1$ );  $2$  (if  $Q_1 \leq x \leq Q_2$ ); 3 (if  $Q2 \le x \le Q3$ ); 4 (if  $x > Q3$ ).)
- (4) K-prototypes with Gower distance;
- (5) KAymeans for MIxed Large data(KAMILA) [\[44](#page-14-11)] This clustering algorithm integrates the k-means algorithm and Gaussian-multinomial mixture models. Like k-means, avoids making strict parametric assumptions about continuous variables. Similar to Gaussianmultinomial mixture models, KAMILA efectively balances the contributions of continuous and categorical variables without presetting weights, instead relying on a data-driven density estimator [\[23](#page-13-21)];
- (6) PAM with Gower distance.

Part II: Comparison of DAFI-Gower with three feature importance algorithms as baseline feature importance methods, to evaluate the performance of NMI (see Table [1](#page-6-0) elaborating on the properties of these methods):

- (1) Distance-based on co-occurrence of values (Algo\_ distance) [[19](#page-13-18), [33\]](#page-14-0). It discretized the continuous attributes and calculated the distance between every pair of attribute values for all attributes. Then, they modifed the k-means algorithm to contain the distribution of all categorical values in a cluster.
- (2) Two-stage approach (FR & FS)  $[45]$  $[45]$  $[45]$ . This methodology employs three fundamental strategies: flter, wrapper, and hybrid (a fusion of both flter and wrapper) to identify relevant and non-redundant features. This work introduces a robust and efficient two-phase (i.e., feature ranking and feature selection) method. In the stage of feature ranking, they employed entropy and mutual information to provide a normalization to rank features, and then defne the feature weight as the degree of the unique or non-shared information (entropy minus the normalization value) of an individual feature.
- (3) Standard mutual information (elaborated in Sect. [2.3](#page-3-1)). This measures the amount of information shared between two random variables, quantifying

<span id="page-6-0"></span>**Table 1** Comparison of diferent components of three baseline feature importance algorithms and diferent combinations of DAFI-Gower algorithm



how much knowing one variable reduces uncertainty about the other.

Part III: Comparison of diferent DAFI-Gower combinations (Fig. [1](#page-3-0)) to evaluate the individual components of the technique (see Table [1](#page-6-0) elaborating on the properties of these methods):

- (1) Distance was calculated using modifed Gower distance, and clustering was performed using PAM.
- (2) Distance was calculated using modifed Gower distance and distance adjustment, and clustering was performed using PAM.
- (3) Distance was calculated using modifed Gower distance and feature importance, and clustering was performed using PAM.
- (4) DAFI-Gower distance matrix was calculated using all three components (modifed Gower distance, distance adjustment, and feature importance), and clustering was performed using PAM.

The median ARI values, along with the 25th and 75th quartile, were reported for all statistics. All data analysis was implemented in R. All algorithms were performed with default values, except for the specifed data and the number of clusters. For k-means clustering, the *'nstart'* parameter was set to 10 rather than the default of 1 to improve result stability. The source code of the data analysis is available from the authors in:[\[https://](https://github.com/Pinyan-Liu/DAFI-Gower-Distance) [github.com/Pinyan-Liu/DAFI-Gower-Distance](https://github.com/Pinyan-Liu/DAFI-Gower-Distance) ] [[46\]](#page-14-13).

# **Empirical study settings**

To demonstrate the practical implementation of the DAFI-Gower distance clustering algorithm, we utilized real datasets to evaluate the proposed method's performance against the methods in the three parts described above, following the study design in Fig. [1](#page-3-0).

CVDs are infammatory conditions of the coronary arteries and the leading cause of death globally. In recent decades, investigators have focused on the impact of PD on CVDs, a potential risk factor, promoting the development and instability of arterial atheroma [\[47\]](#page-14-14). To deliver a comprehensive representation of the relationship, we proposed to estimate the association between PD severity following the 2012 Centers for Disease Control and Prevention (CDC)/American Academy of Periodontology (AAP) [[48](#page-14-15)] (see Supplementary Table 5) and CVDs by adjusting for distinct clusters with similar characteristics. We used data from the 2011–2014 National Health and Nutrition Examination Study (NHANES) [\[49](#page-14-16), [50](#page-14-17)], a continuous study conducted by the Centers for Disease Control and Prevention (CDC) to assess the health and nutrition status of the US population who are not in institutions. This study collects large amounts of quantitative and qualitative data using face-to-face interviews, physical evaluations, computerized questionnaires, and laboratory analyses [[50\]](#page-14-17) and was conducted following the Strengthening the Reporting of Observational Studies in Epidemiology guidelines [\[51\]](#page-14-18).

People over 30 were studied due to the availability of data on PD. Information on PD was clinically obtained and available in NHANES. The analysis excluded

participants without complete periodontal exams or complete covariate data. We defned the indicator of CVDs as being diagnosed with either congestive heart failure or stroke  $[52]$ . Information on CVDs was selfreported and available in NHANES. The data set included 3,760 observations with complete data. Sixteen variables (see Supplementary Table 2) were used to generate clusters, including demographic variables, clinical oral health data, and CVD-related variables. The number of clusters was predetermined to be four [\[48](#page-14-15)]. Clustering analysis used the same 13 approaches as the simulation study (Parts I, II, and III). Clustering quality was assessed using descriptive statistics and Silhouette scores measuring cohesion and separation [\[53\]](#page-14-20). Although Silhouette scores should be interpreted cautiously due to their dependence on the selected distance metric and lack of comparability across diferent distances, it is also a well-used tool for descriptive analysis or as one of multiple metrics in assessing clustering outcomes [\[54](#page-14-21)]. Multivariable logistic regression was used to estimate the association between PD and CVDs, adjusting for clusters generated in the previous step. Additionally, feature signifcance calculated using NMI described in Sect. [2.3](#page-3-1) was plotted to show clustering contribution.

# **Results**

#### **Simulation results**

#### *Results on diferent baseline mixed type clustering (part I)*

Figure [2](#page-8-0)a and Supplementary Table 3 show the median ARI index together with the 25th and 75th percentiles on fve mixed type datasets. From the results, the DAFI-Gower distance with PAM performed consistently the best, especially when only a small portion of variables contribute to the clustering formation. Although KAMILA performed as well as DAFI-Gower in simulations 1 and 5, it does not provide feature importance, which is signifcant in our study settings.

#### *Results on diferent feature importance algorithms (part II)*

Figure [2](#page-8-0)b and Supplementary Table 4 (blue background) show the median ARI index together with the 25th and 75th percentiles on fve mixed type datasets. Separate use of distance adjustment or feature importance performed relatively well in specifc settings, but none showed consistent performance.

# *Results on diferent parts of the proposed method (part III)*

Figure [2](#page-8-0)b and Supplementary Table 4 (the yellow part) compare DAFI-Gower distance and PAM clustering to show each part's improvement. The results indicate that both the DAFI-Gower distance and its component (just the distance adjustment factor or only feature importance weights) performed well. When the data included more non-contributable features (simulation 5), DAFI-Gower distance with PAM performed better than all other approaches.

From above, techniques on mixed type data are often better than those on quantitative or categorized data (Table [1](#page-6-0)). Our novel approaches for mixed type variables performed better than existing methods in settings investigated, especially when employing the DAFI-Gower distance with PAM on datasets with more irrelevant features. Our approaches also give feature importance, an advantage over traditional mixed type clustering algorithms for visualization and real-world application.

Results from the additional analysis with cluster sizes of 30, 60, and 90 are shown in Supplementary Tables 7 and 8. The outcomes are consistent with previous findings. DAFI-Gower performs better than all other methods in both the baseline mixed type clustering comparison (Part I) and feature importance algorithms (Part II). In Part III, which compares DAFI-Gower to its individual components, DAFI-Gower ranks frst in simulations 8, 9, and 10—where more irrelevant variables are included—and second in the remaining cases.

# **Empirical study results** *Clustering results*

Figure [3](#page-9-0) presents the silhouette index according to approaches. The new DAFI-Gower distance and PAM clustering approach has the greatest Silhouette score (0.79), suggesting the best cluster cohesion and separation. The baseline mixed type clustering approaches performed worse than feature-importance clustering. The green area of Fig. [3](#page-9-0) demonstrated that distance adjustments and feature importance weights improved clustering performance, but the combination did more.

Descriptive statistics for four clusters and the overall sample were presented in Table [2.](#page-10-0) Four distinct segments were identifed. Cluster 1 is the healthier and younger, with a mean age of  $50.1 \pm 13.8$  years, and has the lowest proportion of obese people (35.3%), 59.9% of non-smokers, and 86.3% non-diabetes. For PD, Cluster 1 also has the highest proportion of healthy people (61.4%) and non-severe PD people (92.8%). Another signifcant characteristic is that Cluster 1 can be treated as "the cluster with no CVDs" with only 1.8% of participants having CVDs. In contrast, Cluster 3 was the least healthy and oldest, with a mean age of 61.5 (SD: 12.3) years; 77.3% of participants were overweight or obese, only 37.9% were non-smokers, and 62.1% were non-diabetic. For PD, Cluster 3 also has more non-severe PD people (13.6%) and is "the cluster with the highest probability of CVDs" with 34.8% of participants having CVDs. Cluster 2 and 4 are the relatively intermediate ones.



<span id="page-8-0"></span>**Fig. 2** Simulation results of median ARI with 25th and 75th quartile. The frst and second ranks are indicated by green and orange boldface, respectively. **a** Results on comparing diferent baseline mixed type clustering techniques (Part I). **b** Results on comparing diferent baseline feature importance techniques (Part II) and the comparison of diferent DAFI-Gower combinations (Part III)



<span id="page-9-0"></span>**Fig. 3** Comparative analysis of clustering performance using the silhouette index across baseline and novel methods on NHANES data. The graph delineates method categories through color diferentiation

Figure [4](#page-11-0) shows clustering-related feature contributions to help assess cluster characteristics. From the fgure, coronary heart disease, angina pectoris, heart attack, and emphysema are among the averaged contributions, which are all CVD-related. Cluster 1's low CVD prevalence may be explained by the top four features.

### *Association between PD and CVDs*

To investigate the benefts of using clusters in analyzing the association between PD severity (categorized as nonsevere: combining none, mild, and moderate stages; and severe stage) and CVD cases, we conducted three logistic regression analyses: Model 1 - unadjusted analysis; Model 2 - conventional adjusted analysis (that adjusted for individual characteristics); Model 3 - proposed adjusted analysis (that adjusted for cluster membership instead of individual characteristics). From Table [3,](#page-11-1) we found that the association between PD and CVDs reveals signifcant insights in Model 1 (odds ratio (OR) 1.97, 95% confidence interval (CI) 1.55 to 2.49,  $p = 0.0045$ ) but not in Model 2, which indicates that adjusted for too many confounders may diminish the observed association supported by domain knowledge and previous research [\[47](#page-14-14)]. However, this issue can be resolved by adjusting for cluster membership, which provides a more accurate representation of the data indicated by Model 3 (adjusted OR 1.95, 95% CI 1.50 to 2.55, *p*=0.012). Patients diagnosed with severe PD had approximately twice the odds of having CVDs compared to those diagnosed with no PD or non-severe PD.

In addition, after adjusting for clustering, the analysis reveals signifcantly higher CVDs risks in clusters 3 and 4, suggesting that these groups warrant further investigation to identify high-risk populations for targeted interventions in future studies, which is also consistent with the descriptive statistics presented in Table [3](#page-11-1) that clusters 3 and 4 have the signifcantly higher proportions of CVDs cases. This phenomenon suggests that the clusters identifed by the new method may encompass inherent characteristics, possibly undetected or unmeasured risk factors, strongly associated with CVDs risk.

# **DAFI‑Gower algorithm execution time**

Supplementary Table 9, includes the computational cost of DAFI-Gower. The execution times of different algorithms on NHANES, with 3,760 observations and 18 variables, are summarized.

# **Discussion**

In this article, we developed the DAFI-Gower technique, an innovative two-step framework for mixed type clustering to mitigate the limitations of single-type methods and unbalanced measurements like the Gower distance. The novelty of DAFI-Gower lies in its distance adjustment, allowing the same level of contributions for diferent feature types. Additionally, the subsequent inherent feature importance weights, which account for contributions to clustering, enhance the interpretability of the clustering analysis, making it more informative. Results from both simulation and real-world studies demonstrate that the DAFI-Gower distance with PAM clustering is a fexible approach. In real-world studies, DAFI-Gower not only performed well in clustering patients but also helped to improve association studies.

The DAFI-Gower mitigates some limitations of mixed type clustering. Previous studies have often treated continuous and categorical data separately or applied simplistic methods that fail to capture the nuanced

<span id="page-10-0"></span>**Table 2** Descriptive statistics table for four clusters and the overall sample for DAFI-Gower clustering results





<span id="page-11-0"></span>**Fig. 4** Feature importance visualization to account for contributions to clustering

<span id="page-11-1"></span>**Table 3** The coefficient table of the regression analysis

Parameter	Parameter Estimate(B)	Std. Error	OR. (95% CI)	P-value
Model 1	No adjustments			
Intercept	$-3.50$	0.10		$<$ 2e-16 ***
PD severity	0.68	0.24	1.97 (1.55, 2.49)	$0.0045**$
Model 2	Not adjust for clusters, only for individual characteris- tics			
Intercept	0.038	0.97		0.97
PD severity	0.15	0.36	1.16 (0.81, 1.66)	0.68
Model 3	<b>Adjust for clusters</b>			
Intercept	$-4.06$	0.15		$<$ 2e-16 ***
PD severity	0.67	0.27	1.95 (1.50, 2.55)	$0.012*$
Cluster <sub>2</sub>	0.11	0.29	1.11 (0.84, 1.48)	0.70
Cluster 3	3.33	0.30	28.01 (20.83, 37.66)	$<$ 2e-16 ***
Cluster 4	2.99	0.26	19.83 (15.28, 25.74)	$<$ 2e-16 ***

relationships between diferent types of data. For instance, research by Elsie et al. [[55\]](#page-14-22) emphasized the challenges in achieving accurate clustering with mixed data types, often resulting in suboptimal interpretability. Our framework not only acknowledges these challenges but also proposes a robust solution by integrating a novel distance measurement approach that balances the infuence of both data types, as well as considering feature importance to account for feature correlations. This methodological advancement directly responds to the call for more comprehensive analytical tools capable of handling the complexity of modern datasets, as discussed in the works of Amir et al. [\[56](#page-14-23)].

The strengths of the DAFI-Gower technique include its robust performance in scenarios with numerous redundant variables, as evidenced by simulations 4 and 5. In the empirical study using NHANES, the technique achieved superior performance as indicated by the Silhouette index. Moreover, incorporating feature importance enhances the interpretability of the clustering results, allowing better classifcation into high or low-risk CVD groups. Moreover, utilizing clusters in association analyses offers distinct methodological and clinical advantages. In the NHANES study, adjusting for clusters revealed signifcant associations, which is consistent with the well-established consensus that PD is signifcantly associated with CVD [\[47](#page-14-14)], whereas adjusting for individual confounders did not. This approach enhances the robustness and clarity of fndings by reducing multicollinearity, simplifying complex relationships, and improving statistical power. In addition to investigating associations, the magnitude of the coefficients for our clusters indicates substantial variance in CVDs risk, demonstrating the potential of mixed type clustering techniques to uncover nuanced health patterns.

Despite these strengths, our study has limitations. With a time complexity of  $O(n^2)$ , the DAFI-Gower's runtime on NHANES datasets (3,760 observations and 18 variables) is approximately three minutes, which is longer compared to a few seconds for other methods (see Supplementary Table 9). However, it remains acceptable for most real-world clinical applications with moderate cohort sizes, and we will consider optimization strategies to improve efficiency. In addition, some methods were not included as baseline methods due to limitations

of computational capacity. Two commonly used clustering methods are the Latent Class Analysis (LCA) and Latent Class Model (LCM) [[57](#page-14-24), [58](#page-14-25)], which are two statistical techniques used to identify unobserved subgroups (latent classes) within a population based on individuals' responses to observed categorical variables. Although previous research [[57\]](#page-14-24) showed LCM and KAMILA typically performed best in the setting of heterogeneous data, we excluded LCA and LCM in our analysis due to their largest computation time and only included KAMILA as one of the competitors.

For Gower distance, scaling Euclidean distance for continuous features can be improved using methods beyond the interquartile range (IQR). As suggested by D'Orazio [[30\]](#page-13-28), k-nearest neighbor [\[59](#page-14-26)] and kernel density estimator  $[60]$  $[60]$  $[60]$  approaches offer alternative scaling for interval and ratio scale variables. Kernel density estimator scales distances based on density, giving less weight to values in high-density regions and reducing the infuence of outliers by downscaling sparse areas. K-nearest neighbor uses the average distance to each point's nearest neighbors to set a local scale, emphasizing distances within clusters and lessening the impact of extreme values. Although we do not have such variables currently, future studies could explore these methods when such data is collected, providing clinical examples.

Feature importance determination can also be refned. Currently, continuous variables are categorized by quartiles to calculate MI [\[19](#page-13-18), [33](#page-14-0)], but advanced methods allow for MI estimation without discretization. For example, Brian [[61\]](#page-14-28) introduced a non-binning MI estimator for mixed discrete and continuous data, which can also be adapted for Jensen–Shannon divergence, providing a sophisticated measure of feature importance. Additionally, joint data reduction techniques combine dimension reduction and clustering, enabling mixed data clustering with transformed variables on comparable scales [[62\]](#page-14-29). For datasets with diverse feature types, like text, approaches using distortion and convex optimization offer more complex feature weighting [\[63\]](#page-14-30).

Future work may explore more accurate methods for calculating MI for continuous variables. In our study, algorithms were performed with default values for fairness and simplicity; however, optimizing these parameters could further enhance performance. For example, when the number of clusters is not predefned, methods such as the elbow method or prediction strength [[64\]](#page-14-31) can help determine an appropriate cluster count. Additionally, information-based approaches like BIC [\[65](#page-14-32)] could be applied in preprocessing, provided that a suitable likelihood expression is defned. Although this study includes commonly-used clustering methods, future work could expand the comparison to additional algorithms compatible with our proposed Gower distance to provide a more comprehensive evaluation. While this study is limited to hard clustering, future work could explore fuzzy clustering methods, which allow data points to belong to multiple clusters with varying degrees of mem-bership [[66\]](#page-14-33), offering a more flexible clustering approach.

The practical implications of our study are significant. The DAFI-Gower technique's ability to improve cluster quality based on feature importance makes it particularly useful in clinical studies where many measures are taken, but their contributions to outcomes are unclear. Besides, using clusters in association analyses enriches our understanding of disease mechanisms and opens avenues for tailored preventive strategies addressing the multifactorial nature of chronic diseases like CVDs. This approach supports more rational patient subgroups, facilitating personalized treatment plans and improving patient outcomes. Future research should focus on refning the distance measures and feature importance calculations to further improve the technique's performance and applicability in diverse datasets.

# **Conclusion**

This paper introduced DAFI-Gower, an innovative clustering approach for mixed-type datasets that incorporates feature importance to improve cluster quality and interpretability. DAFI-Gower provides a robust tool for identifying meaningful patterns in complex data, supporting data-driven decision-making in epidemiology and other felds requiring efective clustering.

#### **Abbreviations**



#### **Supplementary Information**

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Supplementary Material 1.
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Supplementary Material 2.

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#### **Authors' contributions**

P.L. and M.A.P. conceived and designed the study. P.L. and H.Y. carried out the statistical and computational analyses. P.L. contributed to the design of the study and the interpretation of the fndings. The paper was written by P.L., and revised by Y.N., H.Y., B.C., N.L., and M.A.P. All co-authors have approved the fnal version of the paper.

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#### **Data availability**

The data used in this article can be freely and openly accessed at NHANES. <https://www.cdc.gov/nchs/nhanes/index.htm>Accessed 9 July 2024.

# **Declarations**

#### **Ethics approval and consent to participate**

Health information collected in the NHANES is kept in strictest confdence. During the informed consent process, survey participants are assured that data collected will be used only for stated purposes and will not be disclosed or released to others without the consent of the individual or the establishment in accordance with Sect. 308(d) of the Public Health Service Act (42 U.S.C. 242 m).

#### **Consent for publication**

Not applicable.

#### **Competing interests**

The authors declare no competing interests.

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